

# Fluid substitution for an HTI medium

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# Outline

## ➤ Motivation

3D printed models → fractured rocks, anisotropy and fluid substitution

4D time lapse seismic

## ➤ Experiments

3D printed model, velocity measurements, fluid substitution experiments

## ➤ Theory

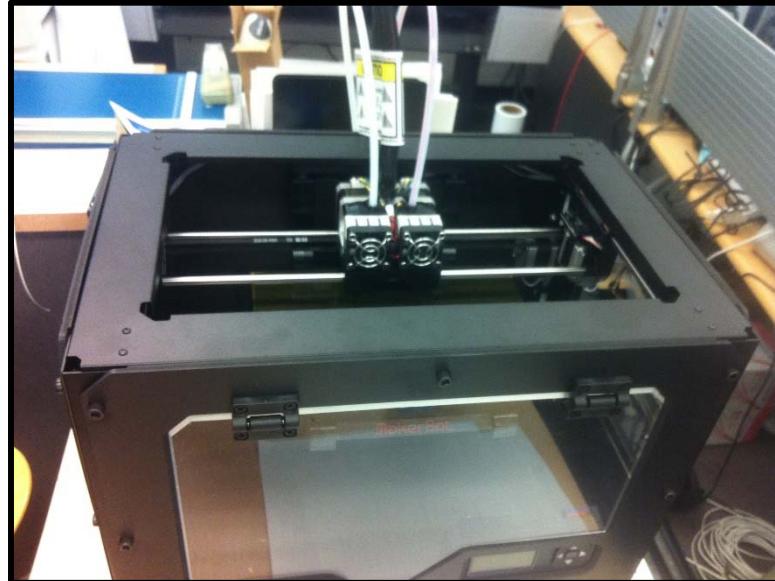
anisotropic Gassmann's equations (recast for an HTI medium)

## ➤ Discussion

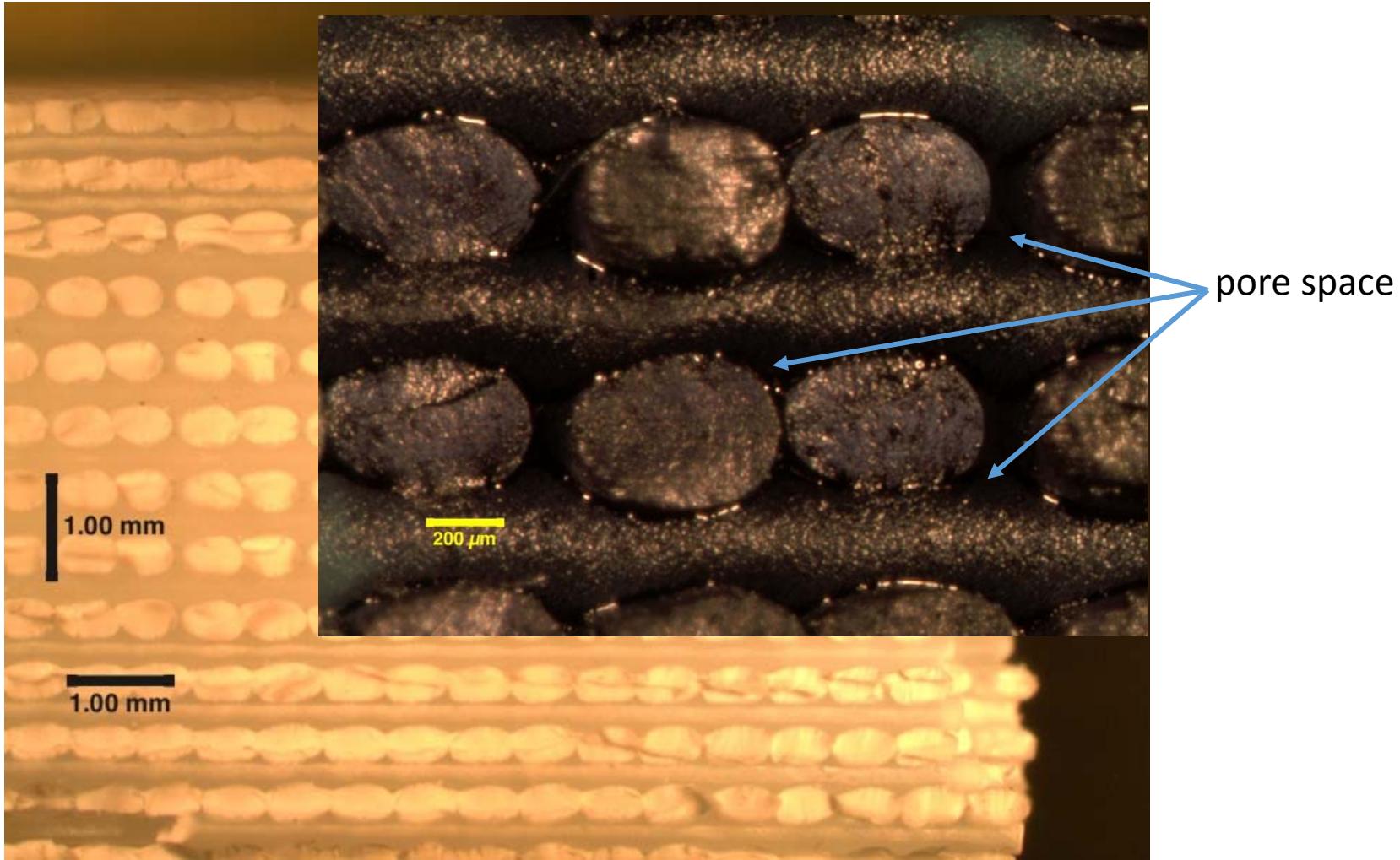
experiment results versus theoretical predictions

## ➤ Conclusions

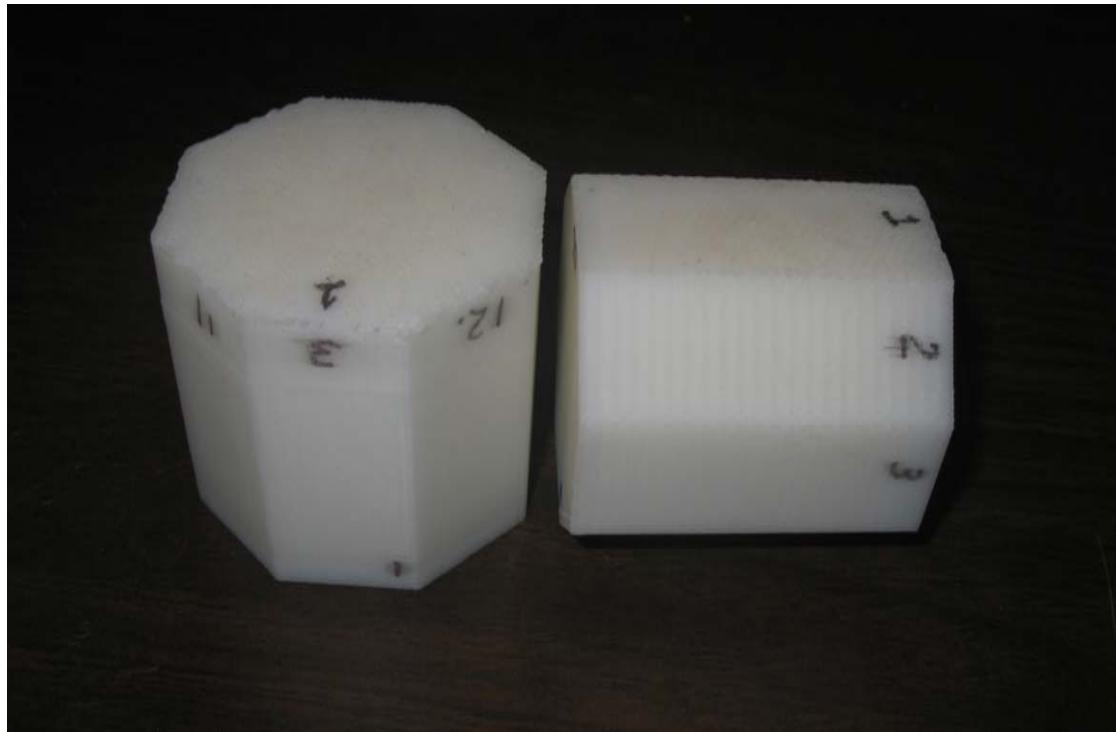
We are the first generation of geophysicists  
to use 3D printed models!



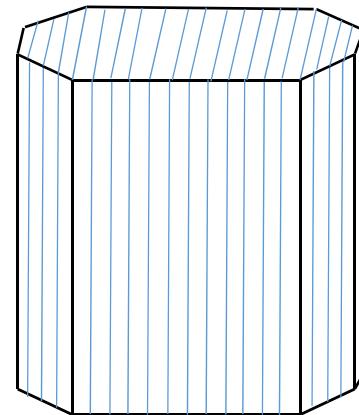
# How it prints and where are the pores?



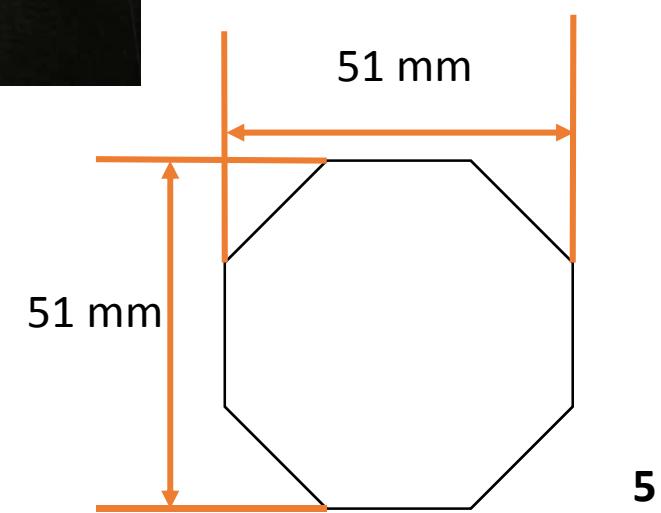
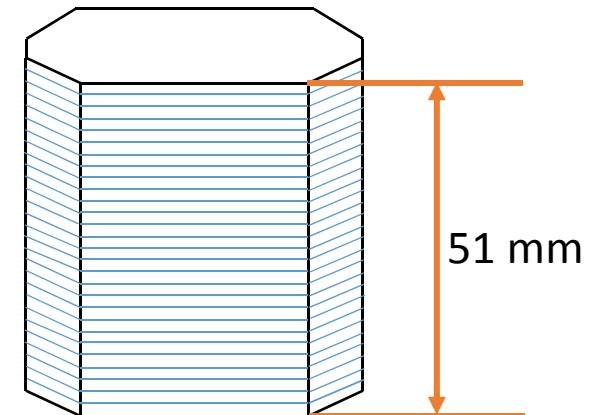
# 3D printed models



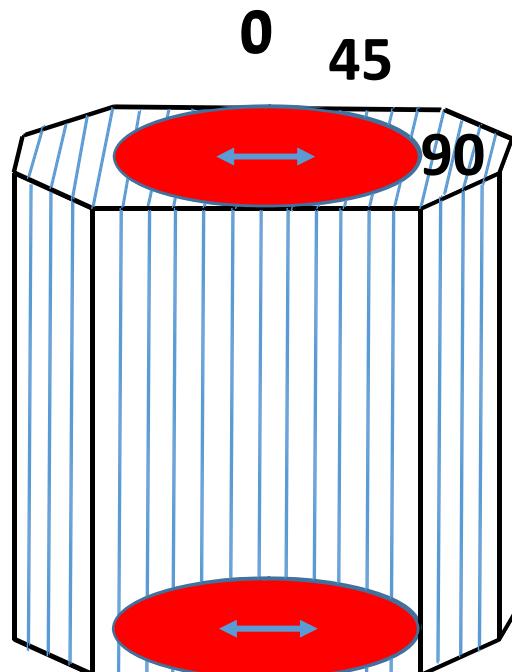
**HTI model**



**VTI model**



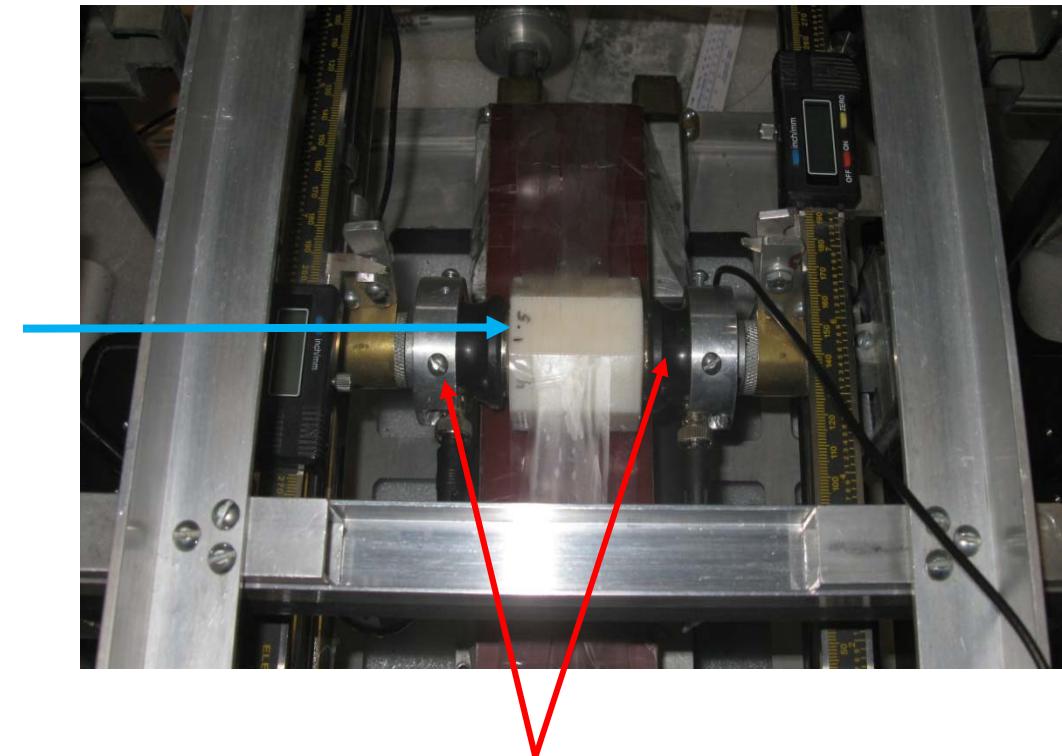
# Rotation experiments



HTI model

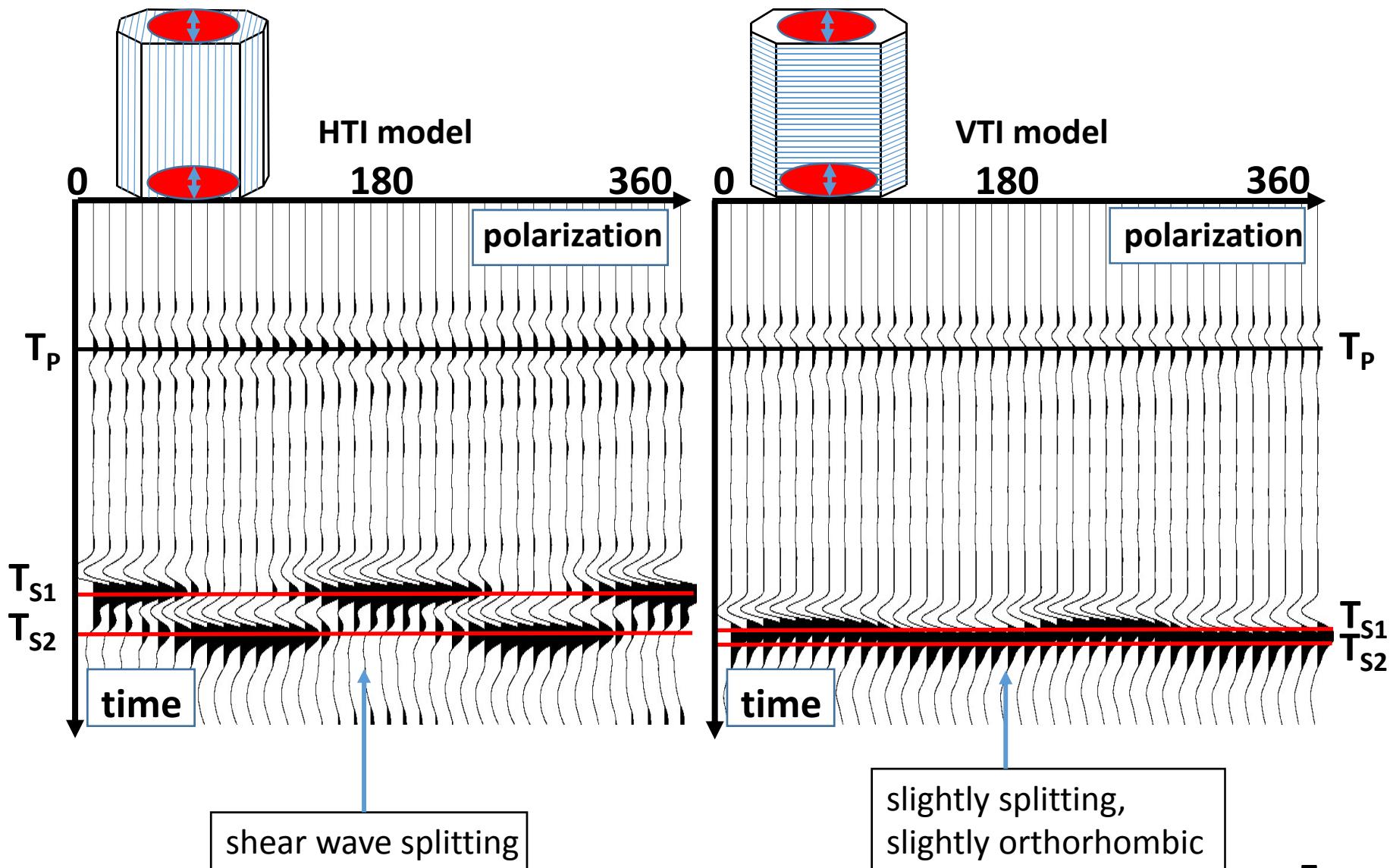


polarization vector



Transducer: 500 kHz horizontal component

# Velocity variation with polarization

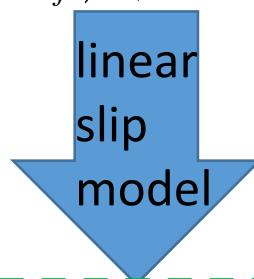


# What if we saturate the models?

- How velocity will change after saturation?  
(P-wave, S-wave?)
- How can we theoretically predict the changes?  
(Gassmann's equations?  
isotropic or anisotropic? VTI, HTI, orthorhombic?  
Hudson's model? Linear slip model? GSA?)
- Why do we care?  
(simulating 4D time lapse seismic!)

# Recast Gassmann's equations

$$C_{ijkl}^{sat} = C_{ijkl}^{dry} + \frac{\left( K_m \delta_{ij} - C_{ij\alpha\alpha}^{dry} / 3 \right) \left( K_m \delta_{ij} - C_{\beta\beta kl}^{dry} / 3 \right)}{\left( K_m / K_{fl} \right) \phi \left( K_m - K_{fl} \right) + \left( K_m - C_{ppqq}^{dry} / 9 \right)} \quad (\text{Gassmann, 1951})$$



(Schoenberg and Sayers, 1995)



$$C_{11}^{sat} = (\lambda + 2\mu)(1 - \delta_N) + \frac{\left( K_m - K_{iso}^{dry} + \delta_N K_{iso}^{dry} \right)^2}{\left( K_m / K_{fl} \right) \phi \left( K_m - K_{fl} \right) + K_m - K_{iso}^{dry} \left( 1 - \delta_N K_{iso}^{dry} / (\lambda + 2\mu) \right)}$$

$$C_{33}^{sat} = (\lambda + 2\mu) \left( 1 - \frac{\lambda^2 \delta_N}{(\lambda + 2\mu)^2} \right) + \frac{\left( K_m - K_{iso}^{dry} + \lambda \delta_N K_{iso}^{dry} / (\lambda + 2\mu) \right)^2}{\left( K_m / K_{fl} \right) \phi \left( K_m - K_{fl} \right) + K_m - K_{iso}^{dry} \left( 1 - \delta_N K_{iso}^{dry} / (\lambda + 2\mu) \right)}$$

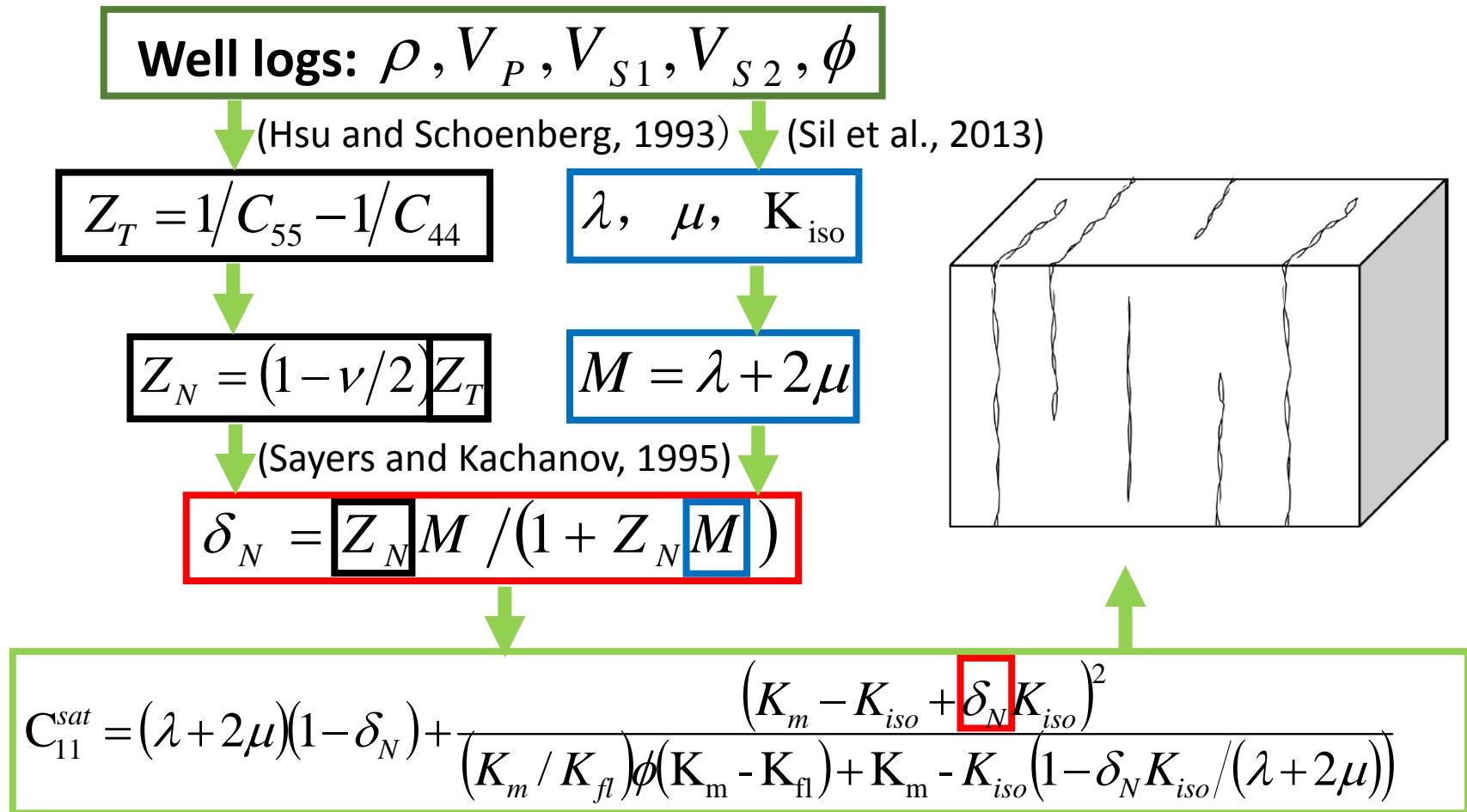
$$C_{44}^{sat} = \mu$$

$$C_{55}^{sat} = \mu(1 - \delta_T)$$

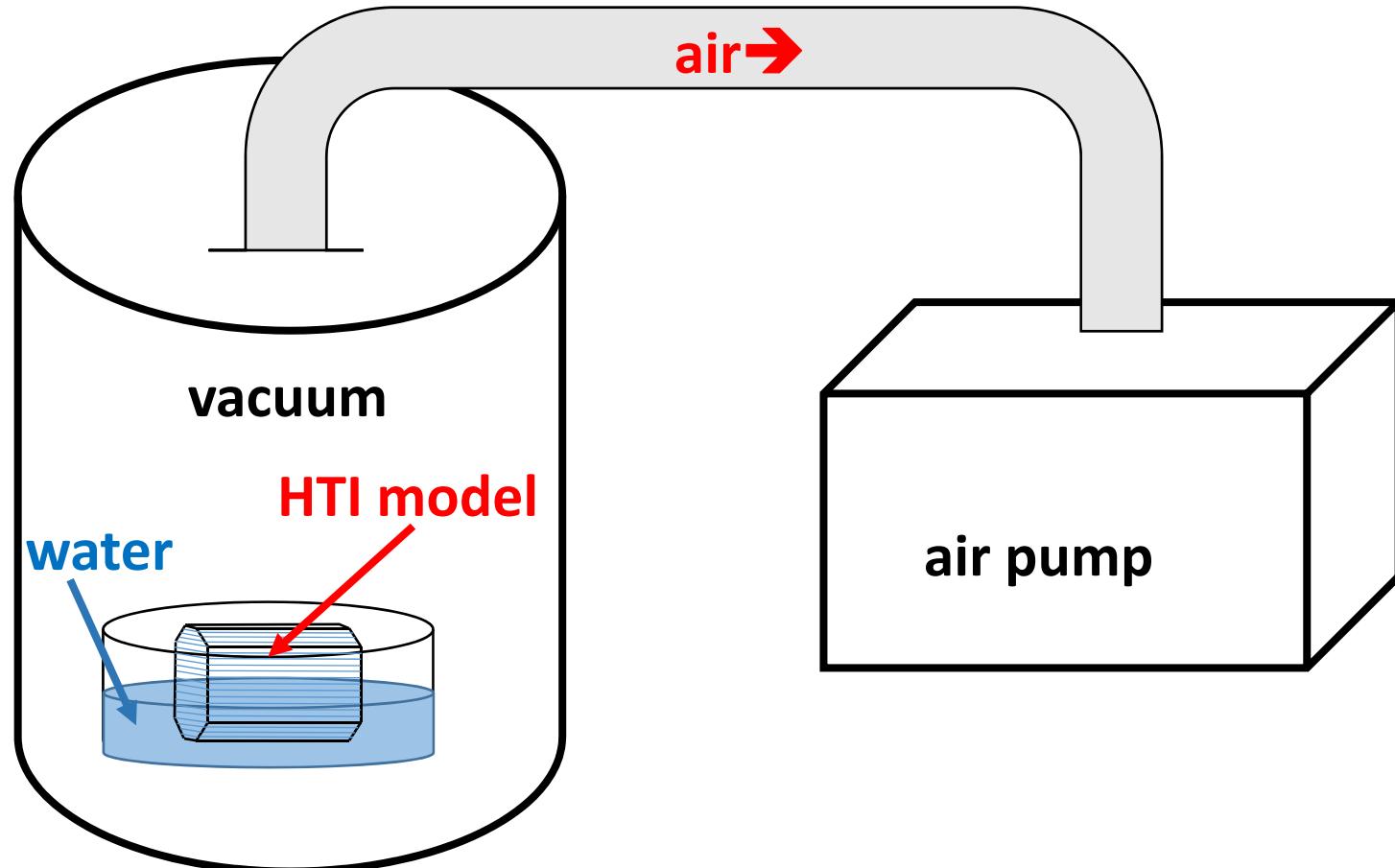
**Dry term**

**Fluid term**

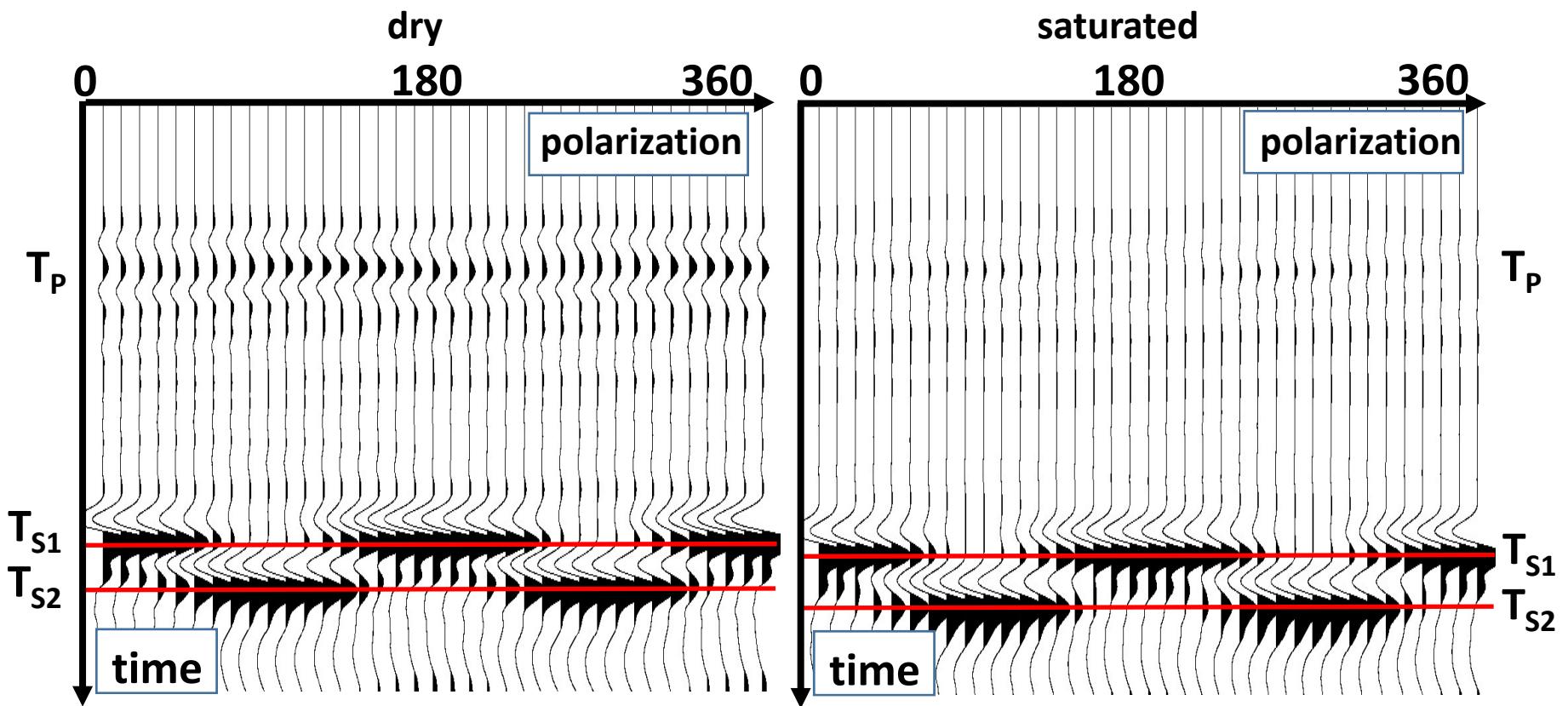
# Parameter estimation



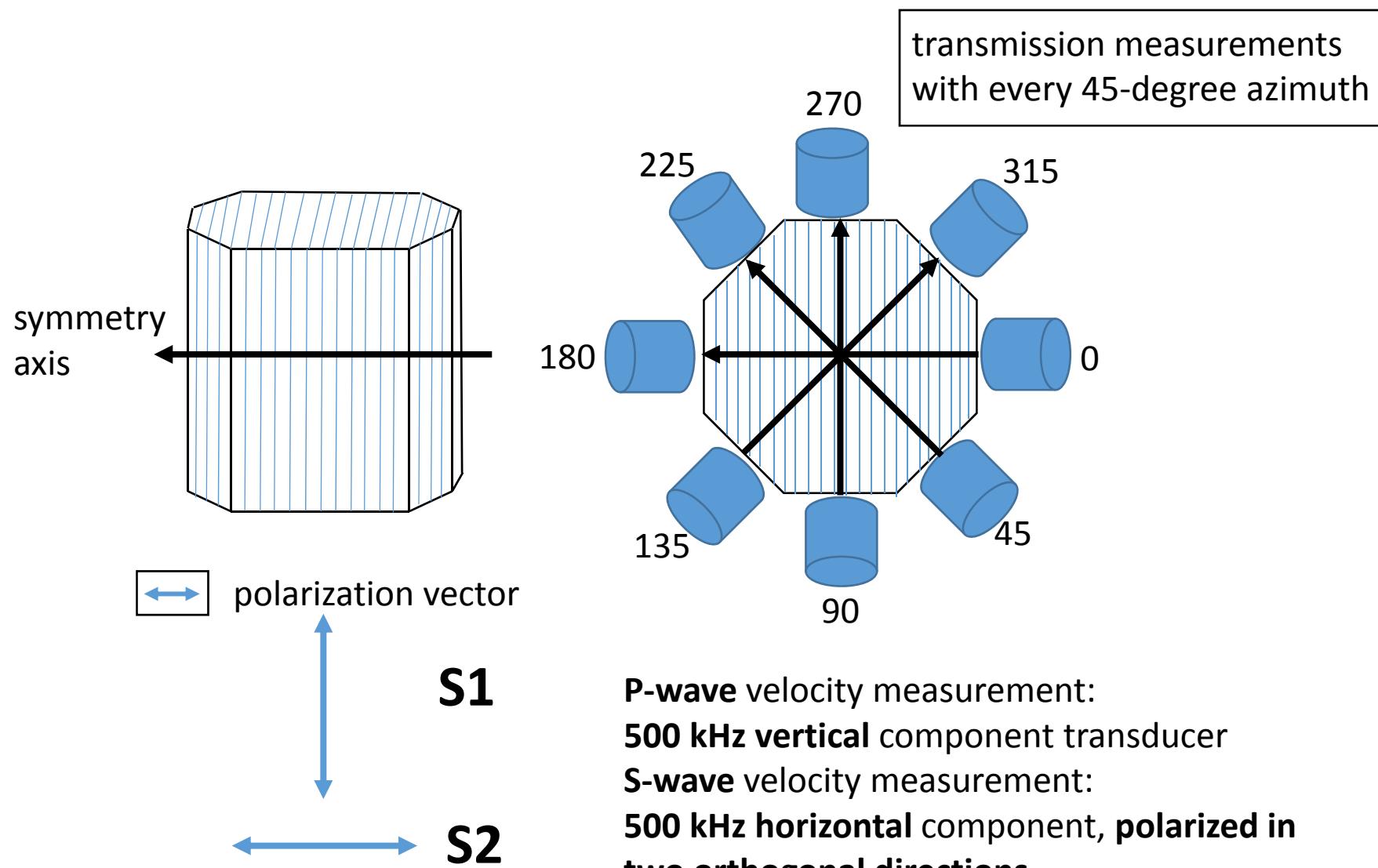
# Fluid substitution experiment (HTI model)



# Fluid substitution



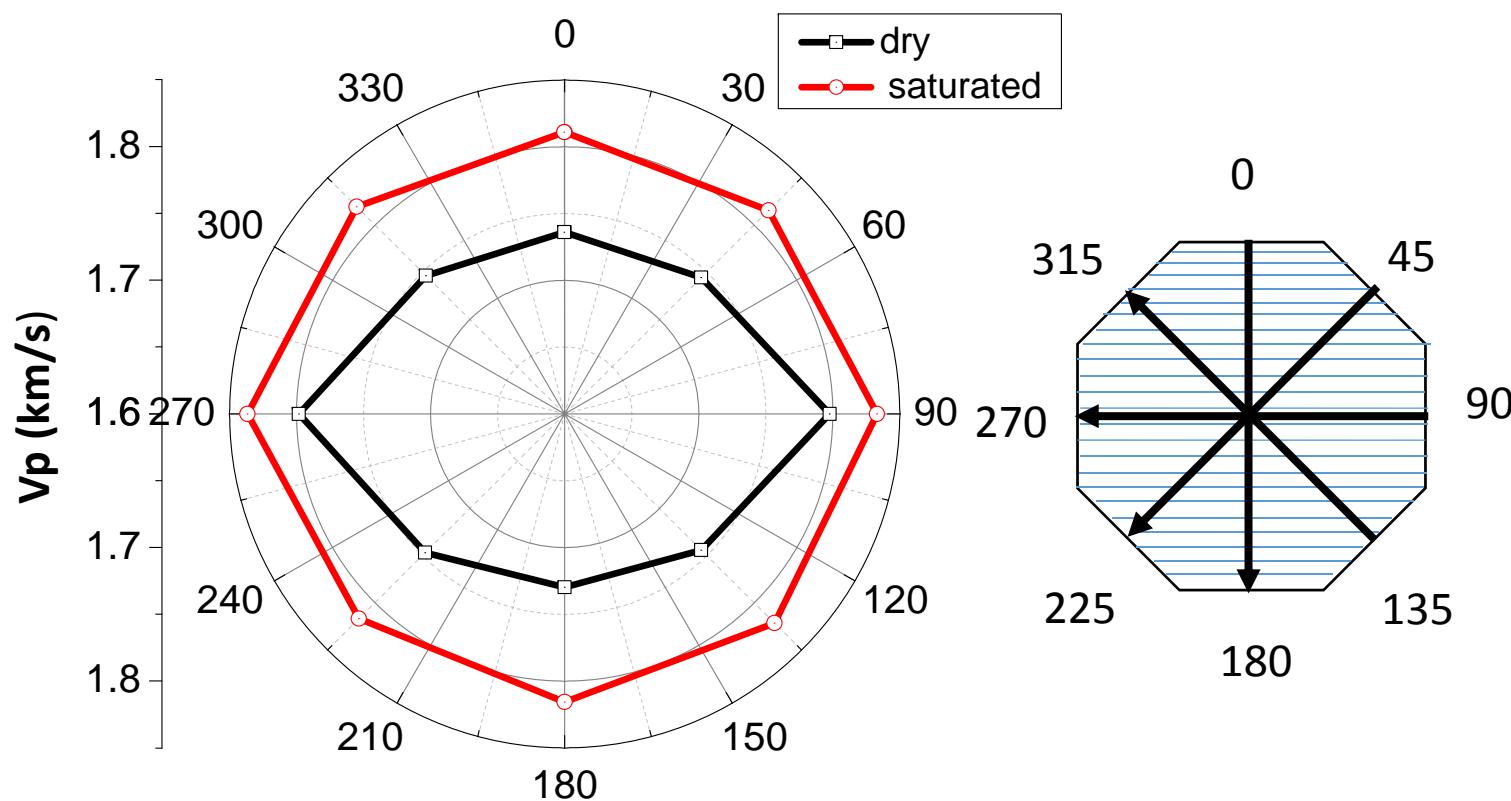
# Velocity measurement from sides



**P-wave velocity measurement:**  
**500 kHz vertical component transducer**

**S-wave velocity measurement:**  
**500 kHz horizontal component, polarized in two orthogonal directions**

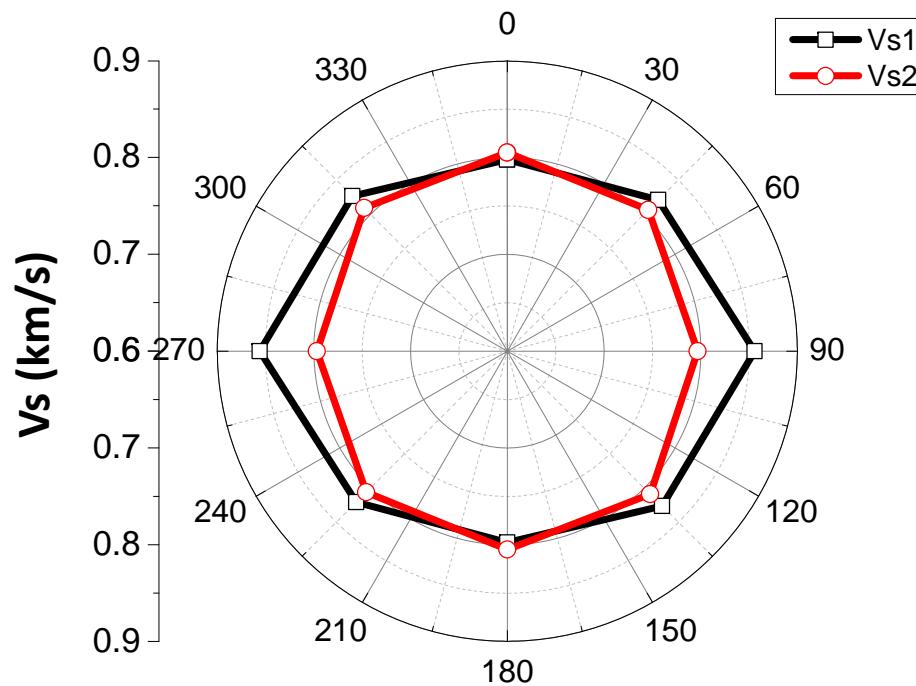
# P-wave velocity change after saturation



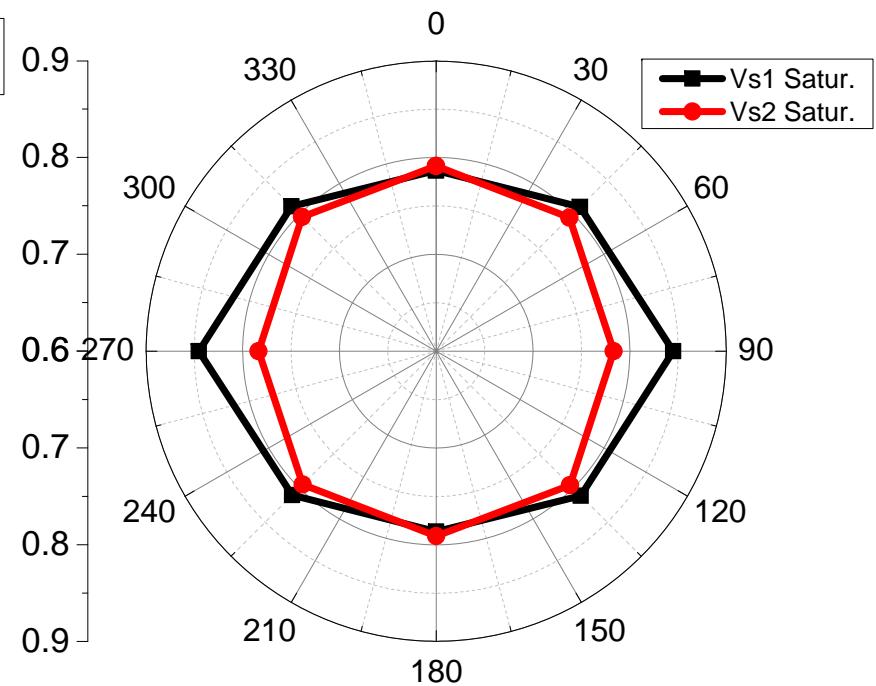
We see 2% - 4.6% increase in P-wave velocity

# S-wave velocity change after saturation

$V_{S1}$  and  $V_{S2}$  before saturation

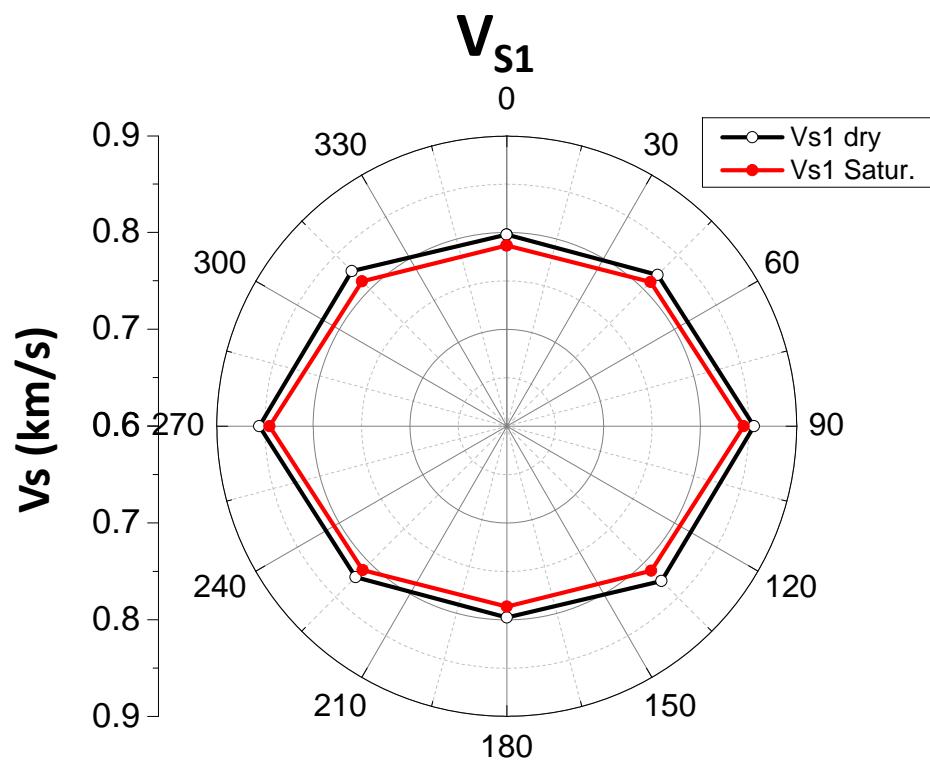


$V_{S1}$  and  $V_{S2}$  after saturation

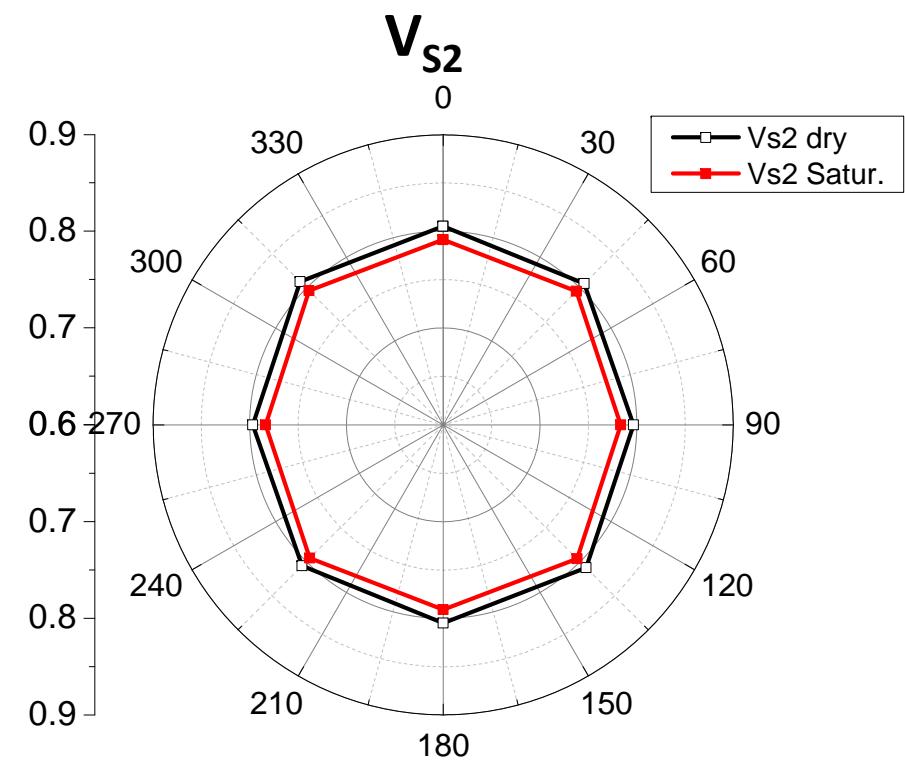


Black denotes fast shear-wave ( $V_{S1}$ )  
Red denotes slow shear-wave ( $V_{S2}$ )

# S-wave velocity change after saturation



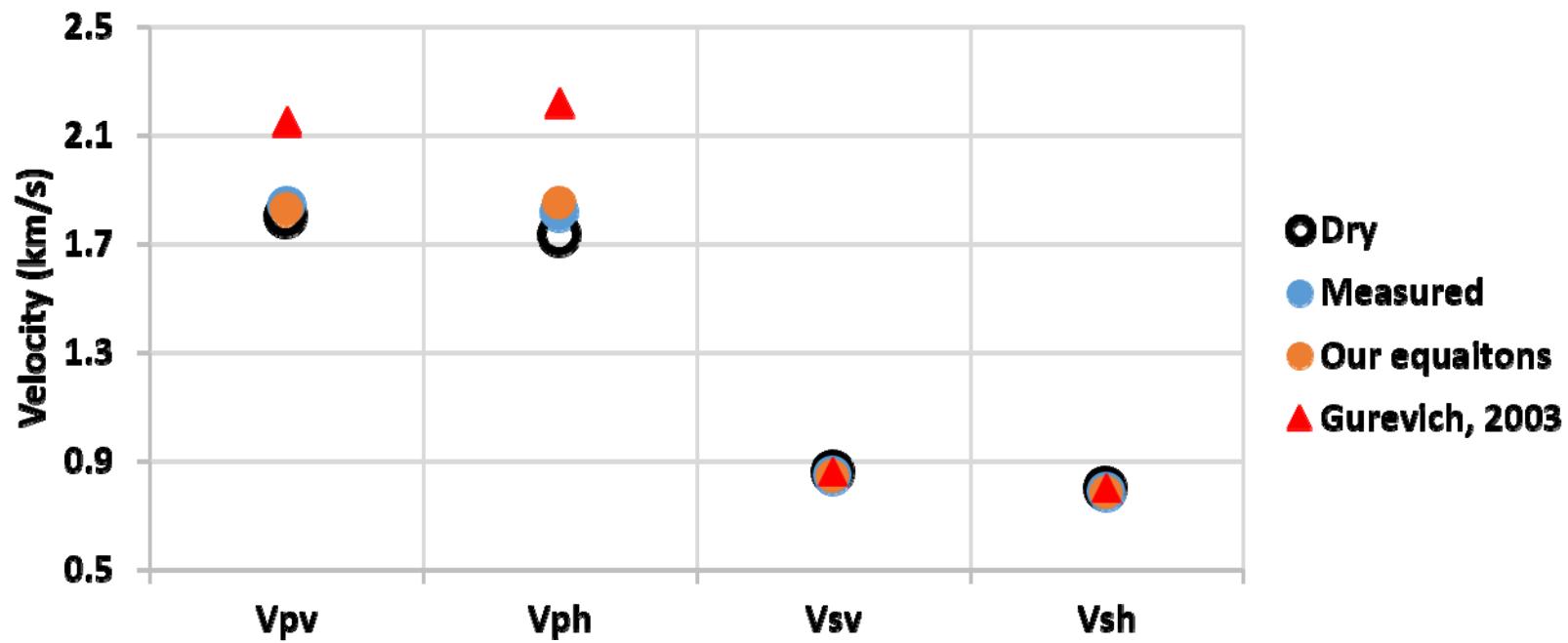
about 1.2% decrease



about 1.6% decrease

Black denotes dry  
Red denotes saturated

# Theoretical predictions for the HTI model



Density increases about 4% after water saturation,  
which contributes about 2% decrease in velocity

# Conclusions

## ✓ Innovative physical models

- print any structure with 3D printing
- cheap and fast.

## ✓ Rich anisotropic response

- transverse isotropic symmetry
- clear shear wave splitting

## ✓ New equations

- Gassmann's equations for an HTI medium
- predict better results for fluid substitution.

# Acknowledgement

- Allied Geophysical Laboratories, UH
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